# Case-Based Reasoning and Analogy: a Turbulent Love Story 

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## ATA@ICCBR-2023

## CBR and analogy: an RCC8 view



## Overview

- Preliminaries:
- Some definitions about CBR
- Some definitions about analogy
- A subjective chronological viewpoint
- CBR examined from the viewpoint of proportional analogies
- Using analogical proportions for reasoning with cases
- Adaptation knowledge learning and analogy
- Is there a way to conclude this talk?


## Preliminaries

Warning:

- To the CBR-ians: the first part is boring for you.
- To the analogists: the second part is boring for you.
- To all: please wake up after the preliminaries!
- In all generality:
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- If there is an exact match of a source case to the query: DB
- Else, requires some inexact matching and adaptation.


## CBR (2/4)

The process model: 2Rs from the 4Rs

$$
\mathrm{x}^{\mathrm{tgt}}
$$

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$$
k \times \mathrm{x}^{s} \longleftarrow \quad \text { retrieval } \mathrm{x}^{\mathrm{tgt}}
$$

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## CBR (3/4)

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- AK: adaptation knowledge (e.g. adaptation rules)
- RK: retrieval knowledge
(e.g. distance function or similarity measure on $\mathcal{P}$ )
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- There are some technological studies on CBR.


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- In particular, analogical proportions.


## Analogical proportions (1/4)

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But you can disagree! (If you dare...)

## Analogical proportions (2/4)

## A set of non-independent postulates

$$
\begin{aligned}
& \text { **** } a: b:: a: b \\
& * * * * ~ a: a:: b: b \\
& * * * \text { If } a: b:: a: x \text { then } x=b \\
& * * * \text { If } a: a:: b: x \text { then } x=b \\
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& \text { *** If } a: b:: c: d \text { then } d: b:: c: a \\
& \text { ** If } a: b:: c: d \text { and } c: d:: e: f \text { then } a: b:: e: f
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- Depending on the analogical proportion, an analogical equation may have 0,1 , more than 1 solution(s).


## Analogical proportions (4/4)

## Examples of analogical proportions

- Arithmetical analogical proportions:

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a: b:: c: d \text { if } b-a=d-c
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(parallelogram abdc)

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- Yves Lepage's analogy on strings

A subjective chronological viewpoint

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In parallel:

- Childhood of CBR

Ch. Riesbeck and R. G. Schank, Inside Case-Based Reasoning, 1989 (MOPs, CHEF, etc.)

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- At that time, analogy $\simeq C B R$


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- Late 1980s, a French group of researchers worked on analogy D. Coulon, J.-F. Boivieux, L. Bourrelly, L. Bruneau, E. Chouraqui, J.-M. David, C. R. Lu, M. Py, J. Savelli, B. Séroussi, C. Vrain, Le raisonnement par analogie en intelligence artificielle, 1990


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Two parallel phenomena within the ICCBR community during the 1990s (subjective view)

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adaptation adaptation

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CBR examined from the viewpoint of proportional analogies

If $a: b:: c: d$ then $a: c:: b: d$


If $a: b:: c: d$ then $a: c:: b: d$


- Horizontal view: $\mathrm{x}^{s}: \mathrm{x}^{\text {tgt }}:: \mathrm{y}^{s}: \mathrm{y}^{\text {tgt }}$

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- Vertical view: $\mathrm{x}^{s}: \mathrm{y}^{s}:: \mathrm{x}^{\text {tgt }}: \mathrm{y}^{\text {tgt }}$

If $a: b:: c: d$ then $a: c:: b: d$


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## Reflexivity-related postulates

|  | TA | DA |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |

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| :---: | :---: | :---: |
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| $a: a:: b: b$ | $\mathrm{x}^{s}: \mathrm{x}^{s}:: \mathrm{y}^{s}: \mathrm{y}^{s}$ | - |
|  |  |  |
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| $a: a:: b: b$ | $\mathrm{x}^{s}: \mathrm{x}^{5}:: \mathrm{y}^{s}: \mathrm{y}^{s}$ | - |
| if $a: b:: a: x$ then $x=b$ | - | if $x^{s}: y^{s}:: x^{s}: y$ then $y=y^{s}$ (unicity of solution) |

## Reflexivity-related postulates

|  | TA | DA |
| :---: | :---: | :---: |
| $a: b:: a: b$ | - | $\mathrm{x}^{s}: \mathrm{y}^{s}: \mathrm{x}^{s}: \mathrm{y}^{s}$ |
| $a: a:: b: b$ | $\mathrm{x}^{s}: \mathrm{x}^{s}:: \mathrm{y}^{s}: \mathrm{y}^{s}$ | - |
| if $a: b:: a: x$ <br> then $x=b$ | - | if $\mathrm{x}^{s}: \mathrm{y}^{s}:: \mathrm{x}^{s}: y$ <br> then $y=\mathrm{y}^{s}$ <br> $($ unicity of solution) |
| if $a: a:: b: x$ <br> then $x=b$ | if $\mathrm{x}^{s}: \mathrm{x}^{s}:: \mathrm{y}^{s}: y$ <br> then $y=\mathrm{y}^{s}$ <br> (unicity of solution) |  |

If $a: b:: c: d$ and $c: d:: e: f$ then $a: b:: e: f$
Multi-step single adaptation using similarity paths and adaptation paths

$$
x^{t g t}
$$

If $a: b:: c: d$ and $c: d:: e: f$ then $a: b:: e: f$
Multi-step single adaptation using similarity paths and adaptation paths

$$
\mathrm{x}^{s} \mathrm{x}^{\mathrm{tgt}}
$$

If $a: b:: c: d$ and $c: d:: e: f$ then $a: b:: e: f$
Multi-step single adaptation using similarity paths and adaptation paths

$$
x^{5} \longrightarrow x^{1} \longrightarrow x^{2} \longrightarrow x^{\text {tgt }}
$$

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Multi-step single adaptation using similarity paths and adaptation paths


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Other postulates of proportional analogies considered from a CBR viewpoint

This is your homework.

## Using analogical proportions for reasoning with cases

## For $k=1$ : principle

- For some applications: $\mathcal{P}=\mathcal{S}$


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Retrieval: select the $\left(\mathrm{x}^{5}, \mathrm{y}^{5}\right) \in \mathrm{CB}$ such that $\mathrm{x}^{5}: \mathrm{y}^{5}:: \mathrm{x}^{\mathrm{tgt}}: y$ is solvable

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R Retrieval: select the $\left(\mathrm{x}^{5}, \mathrm{y}^{5}\right) \in \mathrm{CB}$ such that $\mathrm{x}^{5}: \mathrm{y}^{5}:: \mathrm{x}^{\text {tgt }}: y$ is solvable

- Solve the $\mathrm{x}^{5}: \mathrm{y}^{\text {s }}:: \mathrm{x}^{\text {tgt }}: y$ equations and combine / vote


## For $k=1$ : TFC

Lepage, Lieber, Mornard, Nauer, Romary, Sies, ICCBR-2020, The French Correction: When Retrieval Is Harder to Specify than Adaptation

- Using the analogical proportion (= proportional analogy?) of Yves [Lepage, Denoual, 2005]


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- An English example:

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\begin{aligned}
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\mathrm{x}^{\mathrm{gt}} & = \\
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- For this example: adaptation is simple, retrieval is harder...


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$$

- For this example: adaptation is simple, retrieval is harder...
- Lot of work to do to improve this application... (May be a challenge?)


## For $k=1$ : Correcting image segmentation

Duck, Schaller, Auber, Chaussy, Henriet, Lieber, Nauer, Prade, ICCBR-2022, Analogy-based post-treatment of CNN image segmentations


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## For $k=3$ : principle

- Analogical extrapolation:

$$
\mathrm{x}^{a}: \mathrm{x}^{b}:: \mathrm{x}^{c}: \mathrm{x}^{\mathrm{tgt}}
$$

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- Analogical extrapolation:

$$
\frac{\mathrm{x}^{a}: \mathrm{x}^{b}:: \mathrm{x}^{c}: \mathrm{x}^{\mathrm{tgt}}}{\mathrm{y}^{a}: \mathrm{y}^{b}:: \mathrm{y}^{c}: \mathrm{y}^{\mathrm{tgt}}}
$$

## For $k=3$ : principle

- Analogical extrapolation:

$$
\frac{x^{a}: x^{b}:: x^{c}: x^{\mathrm{tgt}}}{\mathrm{y}^{a}: \mathrm{y}^{b}:: \mathrm{y}^{c}: \mathrm{y}^{\mathrm{tgt}}}
$$

Requires two analogical proportions: on $\mathcal{P}$ and on $\mathcal{S}$

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$$

- Requires two analogical proportions: on $\mathcal{P}$ and on $\mathcal{S}$
- Retrieval: find $\left(\mathrm{x}^{a}, \mathrm{y}^{a}\right),\left(\mathrm{x}^{b}, \mathrm{y}^{b}\right),\left(\mathrm{x}^{c}, \mathrm{y}^{c}\right) \in \mathrm{CB}$ such that $\mathrm{x}^{a}: \mathrm{x}^{b}:: \mathrm{x}^{c}: \mathrm{x}^{\mathrm{tg} \mathrm{t}}$


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- Adaptation: solve the equations $\mathrm{y}^{a}: \mathrm{y}^{b}:: \mathrm{y}^{c}: y$ (and combine solutions, or vote, if there are several solvable equations)


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- Analogical extrapolation:

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- Adaptation: solve the equations $\mathrm{y}^{a}: \mathrm{y}^{b}:: \mathrm{y}^{c}: y$ (and combine solutions, or vote, if there are several solvable equations)
- For arithmetical analogical proportions, retrieval can be implemented efficiently thanks to an offline storage of $x^{b}-x^{a}$ in a database.


## For $k=3$ : case-based translation in 2005

Yves Lepage and Étienne Denoual, Purest ever example-based machine translation: Detailed presentation and assessment, Machine Translation, 2005
$>\mathrm{x} \in \mathcal{P}$ : sentence in an origin language (e.g. French)
$\mathrm{y} \in \mathcal{S}:$ sentence in a destination language (e.g. English)
$\mathrm{x} \rightsquigarrow \mathrm{y}: \mathrm{x}$ can be translated into y

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$>$ Example:

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\begin{aligned}
\mathrm{x}^{a} & = \\
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\begin{aligned}
\mathrm{x}^{a} & = \\
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\mathrm{x}^{c} & = \\
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\mathrm{x}^{a} & =\text { Tu peux le faire aujourd'hui. } \\
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\mathrm{x}^{\mathrm{tgt}} & =\text { Je veux faire du vélo. } \\
\mathrm{y}^{a} & =\text { You can do it today. } \\
\mathrm{y}^{b} & =\text { You want to do it. } \\
\mathrm{y}^{c} & =\text { I can ride my bicycle today. } \\
\mathrm{y}^{\mathrm{tgt}} & =
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\end{aligned}
$$

- [Lepage and Lieber, ICCBR-2018]: (1) recognizing this contribution as a knowledge-light CBR system (2) See how it might be improved into a knowledge-intensive CBR system


## For $k=3$ : work with Emmanuel Nauer, Henri Prade and

 Gilles Richard@ICCBR-2018 Theoretical and empirical study of approximation $(k=1)$, interpolation $(k=2)$ and extrapolation $(k=3)$

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@ICCBR-2018 Theoretical and empirical study of approximation $(k=1)$, interpolation $(k=2)$ and extrapolation ( $k=3$ )
©ICCBR-2019 Competence of pairs of cases (based on support and confidence)
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@ICCBR-2021 When Revision-Based Case Adaptation Meets
Analogical Extrapolation

## For $k=3$ : case-based cleaning <br> Éric Astier, Hugo lopeti, Jean Lieber, Hugo Mathieu Steinbach, Ludovic Yvoz, Case-Based Cleaning of Text Images, ICCBR-2023

$>\mathrm{x} \in \mathcal{P}$ : image of a French text (from 19th or 20 th century) $\mathrm{y} \in \mathcal{S}$ : parameter triple of a cleaning filter $\mathrm{x} \rightsquigarrow \mathrm{y}$ : the cleaning of x with parameter triple y gives satisfying results

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- Approaches based on:
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- Extrapolation $(k=3)$
- Talk on Thursday!

Adaptation knowledge learning and analogical extrapolation

## Adaptation Knowledge Learning (AKL)

- Seminal paper of M. T. Keane and K. Hanney (EWCBR-96) many contributors to AKL (I have started a list, but it is better to have an empty list then a nonempty incomplete liste)


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- The difference heuristics (term borrowed to David Leake)
- From $\left(\mathrm{x}^{i}, \mathrm{y}^{i}\right),\left(\mathrm{x}^{j}, \mathrm{y}^{j}\right)$ two different source cases:
- $\left(\mathrm{x}^{i}, \mathrm{x}^{j}\right) \mapsto \Delta \mathrm{x}^{j j}$ (in some problem difference formalism)
$\downarrow\left(\mathrm{y}^{i}, \mathrm{y}^{j}\right) \mapsto \Delta \mathrm{y}^{j j}$ (in some solution difference formalism)


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- $\left(\mathrm{x}^{i}, \mathrm{x}^{j}\right) \mapsto \Delta \mathrm{x}^{j j}$ (in some problem difference formalism)
$\nabla\left(\mathrm{y}^{i}, \mathrm{y}^{j}\right) \mapsto \Delta \mathrm{y}^{j j}$ (in some solution difference formalism)
$-\operatorname{AKL}:\left\{\left(\Delta \mathrm{x}^{i j}, \Delta \mathrm{y}^{i j}\right)\right\}_{i j} \mapsto \mathrm{AK}$


## AKL with Boolean tuple representation of cases

Generalizable to attribute-value pairs
$\rightarrow$ For $\mathcal{D}=\{=1,=0,+,-\}$

$$
\begin{aligned}
& \mathrm{x}^{i}=\mathrm{x}_{1} \wedge \neg \neg \mathrm{x}_{2} \wedge \mathrm{x}_{3} \wedge \\
& \mathrm{x}^{j}=\mathrm{x}_{1} \wedge \mathrm{x}_{4} \\
& \neg \mathrm{x}_{2} \\
& \wedge
\end{aligned} \mathrm{x}_{3} \wedge \stackrel{\mathrm{x}_{4}}{ }
$$

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$$
\begin{aligned}
\mathrm{x}^{i} & =\mathrm{x}_{1} \wedge \\
\wedge & \neg \mathrm{x}_{2} \\
\wedge & \neg \mathrm{x}_{3} \\
\mathrm{x}^{j} & \wedge \\
\mathrm{x}^{i j} & =\mathrm{x}_{1}
\end{aligned} \mathrm{x}_{4}
$$

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\mathrm{x}_{2} & \wedge \\
\mathrm{x}_{3} & \wedge \\
\mathrm{x}^{j} & =\mathrm{x}_{4} \\
\Delta \mathrm{x}_{1} & \wedge \\
& \mathrm{x}_{1}=1
\end{aligned}
$$

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$$
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\mathrm{x}^{i} & =\mathrm{x}_{1} \wedge \neg \neg \mathrm{x}_{2} \wedge \\
\mathrm{x}_{3} & \wedge \\
\mathrm{x}^{j} & =\mathrm{x}_{4} \\
\Delta \mathrm{x}_{1} & \wedge \\
\mathrm{x} & =\mathrm{x}_{2} \wedge \mathrm{x}_{1} 1 \\
\mathrm{x}_{3} & \wedge \\
=0 & \neg \mathrm{x}_{4} \\
&
\end{aligned}
$$

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& \wedge \neg \mathrm{x}_{3} \\
& \mathrm{x}_{1} \wedge \\
& \neg \mathrm{x}_{2} \wedge \\
& \mathrm{x}_{3} \wedge \\
& \mathrm{x}_{4} \\
& \Delta \mathrm{x}^{i j}=\mathrm{x}_{1}^{=1} \wedge \mathrm{x}_{2}=0 \\
& \mathrm{x}_{3}^{+}
\end{aligned}
$$

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& \mathrm{x}_{2} \wedge \\
& \mathrm{x}_{3} \wedge \\
& \mathrm{x}_{3}=\mathrm{x}_{4} \\
& \Delta \mathrm{x}^{i j}=\mathrm{x}_{1}^{=1} \wedge \mathrm{x}_{2} \wedge \\
& \mathrm{x}_{2} \wedge \\
& \mathrm{x}_{3} \wedge \\
& \mathrm{x}_{3}^{+} \wedge \mathrm{x}_{4} \\
& \mathrm{x}_{4}^{-}
\end{aligned}
$$

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$$
\begin{aligned}
& \mathrm{x}^{i}=\mathrm{x}_{1} \wedge \\
& \mathrm{x}^{j} \neg \mathrm{x}_{2} \\
& \wedge \neg \mathrm{x}_{3} \\
& \wedge \mathrm{x}_{4} \\
& \mathrm{x}^{i} \mathrm{x}_{1} \wedge \\
& \mathrm{x} \neg \mathrm{x}_{2} \\
& \wedge \mathrm{x}_{3} \\
& \wedge \wedge \\
& \mathrm{x}^{i j} \mathrm{x}_{4}=1 \\
& \mathrm{x}_{2} \wedge \\
& \mathrm{x}_{3}^{+} \wedge \\
& \mathrm{x}_{4}^{-}
\end{aligned}
$$

- Applying FCl extraction program gives birth to conjunctions such as $x_{2}^{+} \wedge x_{3}^{=0} \wedge y_{1}^{=1} \wedge y_{2}^{-}$that can be interpreted as an adaptation rule.


## AKL with Boolean tuple representation of cases

Generalizable to attribute-value pairs
$\rightarrow$ For $\mathcal{D}=\{=1,=0,+,-\}$

$$
\begin{array}{rllllll}
\mathrm{x}^{i} & =\mathrm{x}_{1} & \wedge & \neg \mathrm{x}_{2} & \wedge & \neg \mathrm{x}_{3} & \wedge \\
\mathrm{x}_{4} \\
\mathrm{x}^{j} & =\mathrm{x}_{1} & \wedge & \neg \mathrm{x}_{2} & \wedge & \mathrm{x}_{3} & \wedge \\
\neg \mathrm{x}_{4} \\
\Delta \mathrm{x}^{i j} & =\mathrm{x}_{1}^{=1} & \wedge & \mathrm{x}_{2}^{=0} & \wedge & \mathrm{x}_{3}^{+} & \wedge \\
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l lazy $A K L$ with this $\mathcal{D} \Longleftrightarrow$ analogical extrapolation on $\mathbb{B}^{n}$

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- Emmanuel Nauer, Jean Lieber, Mathieu d'Aquin, Lazy Adaptation Knowledge Learning based on Frequent Closed Itemsets, ICCBR-2023


## Conclusion

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- Two fields of AI with

Differences of approaches, methods, vocabularies

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- Use of analogical proportions for CBR

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## Future directions

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A nice drawing to finish the talk


